

# Hardware-in-the-Loop Testing of an Electrohydraulic Servo System

**Attila Kővári**

Collage of Dunaújváros, kovari@mail.duf.hu

*Abstract: Hardware-in-the-Loop (HIL) test is an effective platform for developing and testing complex real-time systems and allows the engineer to test their control units with greater test coverage compared to physical testing alone. Expensive and unique electrohydraulic servo systems are hard to test but HIL systems provides the complexity of the plant under control using mathematical representation of all related dynamic systems. The servo system consist a double ended symmetrical double-acting hydraulic cylinder loaded with a mechanical system, servo valve, a hydraulic power supply with pump, accumulator and relief valve. The real-time servo system HIL simulator produces real-world electrical interactions for the test of the system. In this paper HIL test was used to examine the dynamic behavior of an electrohydraulic servo system while internal leakage changes at cylinder's piston seal.*

*Keywords: HIL test, hydraulic servo system, modelling, simulation*

## 1 Introduction

Hardware-in-the-Loop (HIL) simulation is a technique that is used increasingly in the development and test of complex real-time systems so the purpose of HIL simulation is to provide an effective platform for developing and testing real-time systems. Hardware-In-the-Loop is a form of real-time simulation. Hardware-In-the-Loop differs from pure real-time simulation by the addition of a real component in the loop and simulation is achieving a highly realistic simulation of equipment in an operational virtual environment. HIL simulation provides an effective platform by adding the complexity of the plant under control to the test platform.

The examined and tested plant is an electrohydraulic servo system which is driven by a Texas Instruments DSP control unit.

## 2 Hardware-in-the-Loop Test

The current industry definition of a Hardware-In-the-Loop system is shown in Figure 1. It shows that the plant is simulated and the control unit is real. The purpose of a Hardware-In-the-Loop system is to provide all of the electrical stimuli needed and a typical HIL system includes sensors, actuators to receive data from the control system, actuators to send data, a controller to process data, a human-machine interface (HMI) and a development post-simulation analysis platform. The value of each electrically emulated sensor is controlled by the plant simulation and is read by the embedded system under test. Likewise, the embedded system under test implements its control algorithms by outputting actuator control signals. Changes in the control signals result in changes to variable values in the plant simulation.

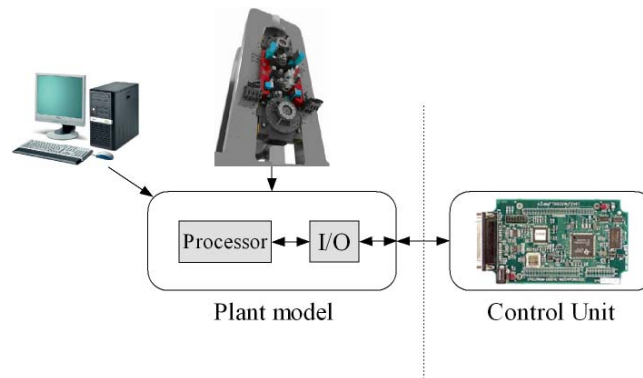


Figure 1  
Hardware-in-the-Loop System

Advantages of HIL systems:

- enable testing the hardware without building a “plant prototype”
- supports reproducible test runs that can assist in uncovering and tracking down hard to find problems
- enables testing less risk of destroying system
- provides cost savings by shortened development time
- complete, consistent test coverage
- supports automated testing
- simulator performs test outside the normal range of operation

The most evident advantage of HIL simulation is that real-world conditions are achieved without the actual risks involved. HIL simulation is achieving a highly

realistic simulation of equipment in an operational virtual environment. With HIL, you can test the control units with extreme conditions that might not be feasible in the real world. HIL enables you to isolate deficiencies in the control unit even if they occur only under certain circumstances. Robust, high-fidelity real-time HIL simulations not only enable shorter time to market by reducing the development period, but also reduce cost by eliminating the need for actual hardware during testing, as well as associated maintenance costs. With the power and flexibility of today's computers, engineers and scientists are increasingly using PC-based systems for HIL simulation applications. A key element of the development of such a system is the integration of signal generation/acquisition I/O functions with the software used to simulate the system. A normal desktop PC was used as hardware of the HIL simulator with a National Instruments PCI-6251 analog-digital data acquisition card. The real-time operating system solution for the plant model was xPC Target real-time kernel.

## 2 Plant and Control Unit

Plant is an electrohydraulic servo system shown in Figure 1 and 2. Electrohydraulic servo actuators are widely used in industrial applications because it has high moving force, power/volume ratio and they proof against environmental impacts so it can be used as built-in element at the acting location directly. Electrohydraulic servos are capable of performance superior to that of any other type of servo. Large inertia and torque loads can be handled with high accuracy and very rapid response. A typical position controlled hydraulic system consists of a hydraulic power supply, flow control valve, linear actuator, displacement transducer, and electronic servo-controller. [1]

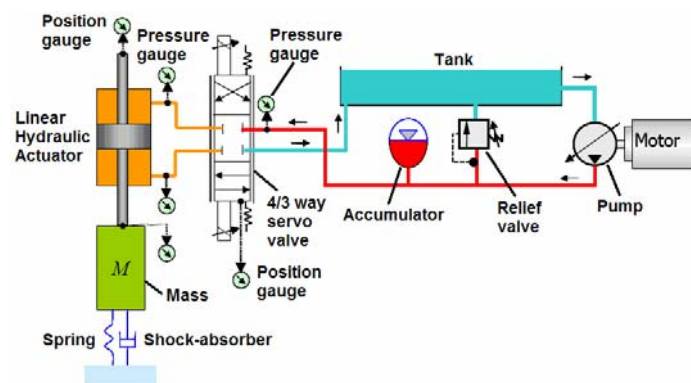


Figure 2  
Electrohydraulic Servo System

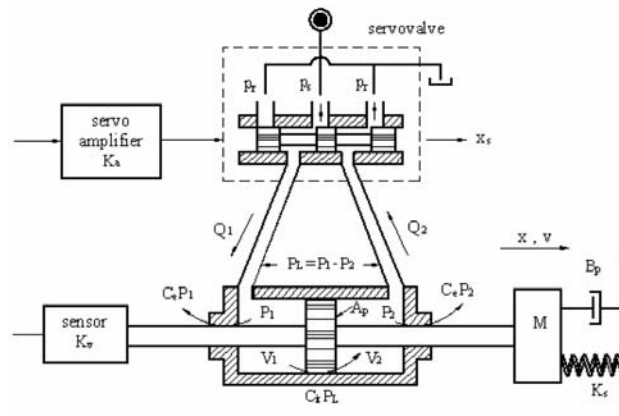


Figure 3

Electromagnetic Driven Servo Valve and Double-acting, Double-ended Linear Hydraulic Actuator

The control unit F2812 eZdsp™ card is a stand alone module with a single chip parallel port to JTAG scan controller. The eZdsp F2812 allows developers to get started using the F2812 DSP. The C28x core is the world highest performance DSP core for digital control applications. The 32-bit F2812 has on board flash, 64K words on board RAM and runs at 150MHz, making it capable of numerous sophisticated control algorithms in real-time. The module can be operated without additional development tools such as an emulator. The combination of a bundled version of Code Composer and an on-board JTAG interface means that the eZdsp can be used to develop and debug code without the requirement for an external emulator or debugger. [2]



Figure 4

eZdsp F2812 Development Package

### 3 Plant Mathematical Model

A servo-valve is a complex device which exhibits a high-order non-linear response, and knowledge of a large number of internal valve parameters is required to formulate an accurate mathematical model. When modeling complex servo-valves, it is sometimes possible to ignore any inherent non-linearities and employ a small perturbation analysis to derive a linear model which approximates the physical system. Such models are often based on classical first or second order differential equations, the coefficients of which are chosen to match the response of the valve based on frequency plots taken from the data sheet. The electrical characteristics of the servo-valve torque motor may be modeled as a series L-R circuit. The transfer function of a series L-R circuit is [4]:

$$L_C \cdot \frac{di}{dt} + R_C \cdot i = K_a \cdot u \quad (1)$$

where  $L_C$  is the inductance of the servo valve coil, and  $R_C$  the combined resistance of the servo valve coil and the current sense resistor,  $K_a$  the amplification of the servo amplifier,  $u$  and  $i$  are the control voltage and current. The lateral force on the valve spool is proportional to torque motor current, but oil flow rate at the control ports also depends upon the pressure drop across the load. The dynamic model of the valve spool may be approximated by a second order transfer function without serious loss of accuracy [4]:

$$\frac{d^2 x_s}{dt^2} + 2 \cdot \zeta_s \cdot \omega_s \cdot \frac{dx_s}{dt} + \omega_s^2 \cdot x_s = \omega_s^2 \cdot k_t \cdot i \quad (2)$$

where  $\omega_s$  is the natural frequency and  $\zeta_s$  damping ratio of the spool,  $k_t$  proportionality coefficient between the control current and valve spool displacement  $x_s$ .

The servo-valve delivers a control flow proportional to the spool displacement for a constant load. For varying loads, fluid flow is also proportional to the square root of the pressure drop across the valve. Control flow, input current, and valve pressure drop are related by the following equations [3,4]:

$$Q_a = Q_{1s} = c_s \cdot w \cdot x_s \cdot \sqrt{\frac{2}{\rho} \cdot (P_s - P_a)} \quad (3)$$

$$Q_b = Q_{2s} = c_s \cdot w \cdot x_s \cdot \sqrt{\frac{2}{\rho} \cdot (P_b - P_T)} \quad (4)$$

$$A_s = w \cdot x_s \quad (5)$$

where  $c_s$  is the volumetric flow coefficient and  $w$  the valve-port width – area gradient,  $A_s$  the size of flow cross-section of the valve,  $\rho$  volumetric density of the

oil,  $P_S$ ,  $P_T$  are system pressure and tank pressure,  $P_a$  and  $P_b$  are the load and return pressure,  $Q_a$  and  $Q_b$  the load and return flow of the valve.

The compressibility of the oil creates a “spring” effect and it can be modeled using the flow continuity equation from fluid mechanics [3,4]:

$$Q_a - Q_b = \frac{dV}{dt} + \frac{V}{\beta} \cdot \frac{dP}{dt} \quad (6)$$

where  $V$  is the internal fluid volume (in pipe and cylinder) and  $\beta$  the fluid bulk modulus. This equation can be used if the mechanical structure is perfectly rigid. The pressures in cylinder chambers are [1,3,4]:

$$\frac{dP_a}{dt} = \frac{dP_1}{dt} = \frac{\beta}{V} \cdot \left( Q_a - \frac{dV_a}{dt} \right) \quad (7)$$

$$\frac{dP_b}{dt} = \frac{dP_2}{dt} = \frac{\beta}{V} \cdot \left( Q_b - \frac{dV_b}{dt} \right) \quad (8)$$

$$\frac{dV_a}{dt} = -\frac{dV_b}{dt} = A_p \cdot \frac{dx}{dt} = A_p \cdot v \quad (9)$$

where  $x$  and  $v$  are the position and speed of the piston and  $A_p$  the active area of the piston annulus. If the sealing is not perfect there is an additional leakage oil flow  $Q_i$  between the chamber “a” and “b” [1]:

$$Q_i = \frac{P_1 - P_2}{R_i} = C_i (P_1 - P_2) \quad (10)$$

$$Q_{e1} = \frac{P_1}{R_{e1}} = C_{e1} P_1, \quad Q_{e2} = \frac{P_2}{R_{e2}} = C_{e2} P_2 \quad (11)$$

$$C_i = \frac{1}{R_i}, \quad C_{e1} = \frac{1}{R_{e1}}, \quad C_{e2} = \frac{1}{R_{e2}} \quad (12)$$

where  $R_i$  and  $R_e$  are the internal and external cylinder’s leakage resistance,  $C_i$  and  $C_e$  the internal and external cylinder’s leakage coefficient. Using equations (7)-(11) the load and return flow  $Q_1$  and  $Q_2$  of the hydraulic actuator and considering the internal fluid volume  $V$  is:

$$V = V_0 + A_p \cdot x \quad (13)$$

$$\frac{dP_1}{dt} = \frac{\beta}{V_0 + A_p \cdot x} [Q_a - A_p \cdot v - Q_i - Q_{e1}] \quad (14)$$

$$\frac{dP_2}{dt} = \frac{\beta}{V_0 - A_p \cdot x} [-Q_b + A_p \cdot v + Q_i - Q_{e2}] \quad (15)$$

where  $V_0$  is the internal fluid volume when the piston is in middle position.

The net force acting on the piston ( $F_p$ ) can be calculated by the differential pressure:

$$F_p = A_p \cdot (P_1 - P_2) \quad (16)$$

Force equation of the piston can be calculated when the load is a mass  $M$ , spring with stiffness coefficient  $K_s$  and a shock absorber with damping ratio  $B_p$ :

$$F_p = (M + M_p) \cdot (a + g) + B_p \cdot v + K_s \cdot x + \text{sign}(v) \cdot F_f \quad (17)$$

where  $M_p$  is the mass of the actuator piston and rod of the actuator,  $g$  gravity,  $F_f$  frictional force,  $a$  acceleration,  $v$  speed and  $x$  position of the piston.

## 4 Test Environment

Plant model runs on a PC using xPC Target real-time kernel and a laptop with MATLAB to generate the code from mathematical model of the electrohydraulic servo system. The PCI-6251 A/D card voltage input is used to control the servo valve and voltage outputs to examine the time functions of the system variables. The control signal of the servo valve was generated by the F2812 DSP board.



Figure 5  
Test Environment

The parameters of the electrohydraulic servo system are:

Symbol	Description	Value
$K_a$	Amplification of the servo amplifier	50
$L_C$	Inductance of the servo valve coil	0.6 H
$R_C$	Combined resistance of the servo valve coil and the current sense resistor	100 $\Omega$
$\zeta_s$	Damping ratio of the spool	0.9
$\omega_s$	Natural frequency of the spool	200 rad/s
$k_t$	Proportionality coefficient between the control current and valve spool displacement	0.01 m/A
$c_s$	Volumetric flow coefficient	0.6
$w$	Valve-port width	$10^{-3}$ m

Table 1  
Parameters of the Flow Control Servo Valve

Symbol	Description	Value
$V_0$	Internal fluid volume when the piston is in middle position	$300 \cdot 10^{-6}$ m <sup>3</sup>
$A_p$	Active area of the piston annulus	$8 \cdot 10^{-4}$ m <sup>2</sup>
$\beta$	Hydraulic fluid bulk modulus	$1.4 \cdot 10^9$ N/m <sup>2</sup>
$R_i$	Internal cylinder's leakage resistance	$10^{12}$ Ns/m <sup>5</sup>
$R_{e1}, R_{e2}$	External cylinder's leakage resistance	$4 \cdot 10^{12}$ Ns/m <sup>5</sup>
$M_p$	Mass of actuator piston and rod	5 kg
$x_{pmax}$	Total stroke of the piston	0.3 m

Table 2  
Parameters of the Actuator

Symbol	Description	Value
$P_S$	System pressure	$210 \cdot 10^5$ Pa
$P_T$	Tank pressure	0 Pa
$\rho$	Volumetric density of the oil	890 kg/m <sup>3</sup>

Table 3  
Parameters of the Power Supply



Symbol	Description	Value
M	Load mass	50 kg
B <sub>p</sub>	Damping ratio	$2 \cdot 10^3$ Ns/m
K <sub>s</sub>	Spring stiffness coefficient	$5 \cdot 10^4$ N/m
F <sub>f</sub>	Frictional force	10 N
g	Gravity	$9.81 \text{ m/s}^2$

Table 4  
 Parameters of the Load

## 5 Test Results

The test execution time was 2s and step response was examined. The observed variables are  $u$  servo valve control voltage,  $x_s$  servo valve spool position (these are independent of  $R_i$ ),  $Q_a$ ,  $Q_b$  load and return flow of the valve,  $P_1$ ,  $P_2$  load and return pressure,  $x$  position of the piston and mass load and  $F_p$  acting force of the hydraulic actuator. Time functions of the electrohydraulic system are shown in the next figures (Fig. 6-12).

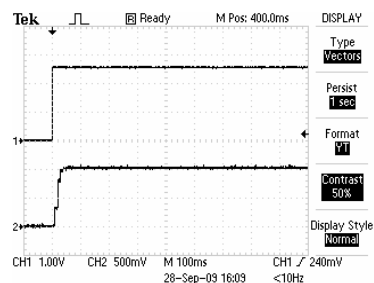


Figure 6

CH1: control voltage  $u(t)$   $K_u=4$ , CH2: position of servo valve spool  $x_s(t)$   $K_{x_s}=0.005\text{m/V}$

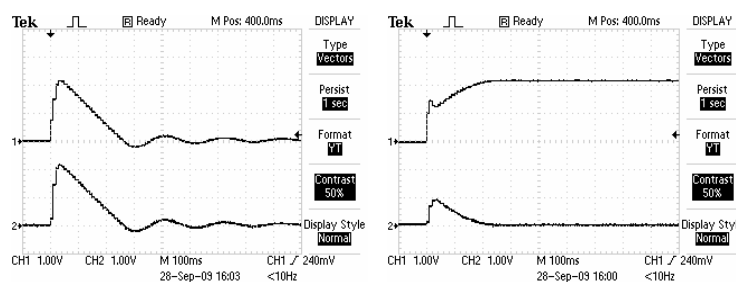


Figure 7 a,b

CH1a:  $Q_a(t)$ , CH2a:  $Q_b(t)$   $K_Q=10^{-3} \text{ m}^3/\text{s/V}$ , CH1b:  $P_1(t)$ , CH2b:  $P_2(t)$ ,  $K_p=10^7 \text{ Pa/V}$  at  $R_{i3}= 10^{12}$

A. Kővári

Hardwer-in-the-Loop Testing of an Electrohydraulic Servo System

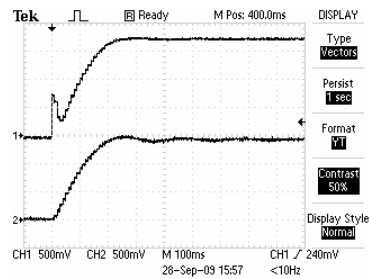


Figure 8

CH1:  $F_p(t)$   $K_{Fp} = 10^4 \text{ N/V}$  and CH2:  $x(t)$   $K_x = 0,25 \text{ m/V}$  at  $R_{i3} = 10^{12}$

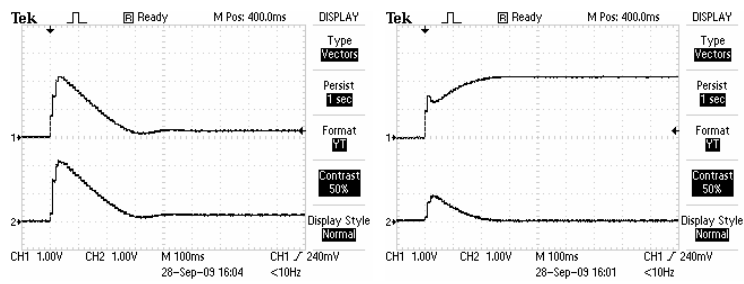


Figure 9 a,b

CH1a:  $Q_a(t)$ , CH2a:  $Q_b(t)$   $K_Q = 10^{-3} \text{ m}^3/\text{s/V}$ , CH1b:  $P_1(t)$ , CH2b:  $P_2(t)$ ,  $K_p = 10^7 \text{ Pa/V}$  at  $R_{i3} = 10^{11}$

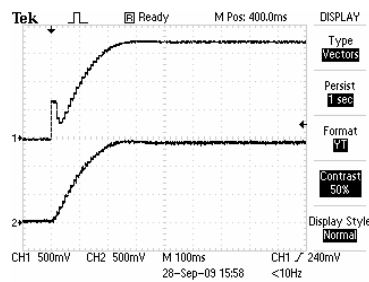


Figure 10

CH1:  $F_p(t)$   $K_{Fp} = 10^4 \text{ N/V}$  and CH2:  $x(t)$   $K_x = 0,25 \text{ m/V}$  at  $R_{i3} = 10^{11}$

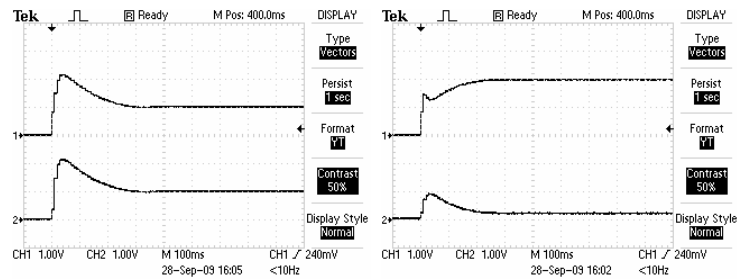


Figure 11 a,b

CH1a:  $Q_a(t)$ , CH2a:  $Q_b(t)$   $K_Q=10^{-3} \text{ m}^3/\text{s}/\text{V}$ , CH1b:  $P_1(t)$ , CH2b:  $P_2(t)$ ,  $K_p=10^7 \text{ Pa}/\text{V}$  at  $R_{i3}=10^{10}$

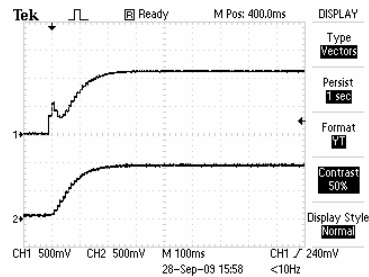


Figure 12

CH1:  $F_p(t)$   $K_{Fp}=10^4 \text{ N}/\text{V}$  and CH2:  $x(t)$   $K_x=0,25 \text{ m}/\text{V}$  at  $R_{i3}=10^{10}$

## Conclusions

It is shown in the step response in Figure 6 that position of servo valve pool rapidly follows the valve control voltage and opens the flow channel to the hydraulic actuator. When the servo valve opens, the oil flow immediately increasing (see Figure 7a) and it causes growing pressure drop in the control valve therefore the load pressure growing period is cracked (see P1 in Figure 7b). When the quantity of oil flow goes on decreasing, the load pressure starts to grow again and reaches the system pressure. Because of the acting force is proportional to load pressure the time function of acting force is similar to load pressure (see Figure 8). After the control valve opening the position of the actuator piston suddenly starts to move therefore the return pressure starts to grow. When the speed of the piston is decelerating the pressure is decreasing (see Figure 7b, P2). It is shown in Figure 8 that the piston is moving rapidly and stops with decreasing oscillation at 0,35m.

It is shown in the step response that 10% cylinder's leakage resistance changing the system's behavior from periodic to aperiodic (See Fig 10). Additionally 20% cylinder's leakage resistance changing decreases the acting force with 30% so the

movement of the actuator is less than 0,25m (Fig. 12). Furthermore it is shown in Fig 11a that high quantity, more than  $10^{-3}$  m<sup>3</sup>/s oil flows from the actuator cylinder chambers “a” to “b” and the maximum pressure in cylinder chamber “a” is less than  $200 \cdot 10^5$  Pa (Fig. 11b).

The presented plant model is capable to examine the dynamic behavior of the described electrohydraulic servo system in real-time, and this model can give a basis for examination of these systems, for example how the system behavior changes when sealing is damaged.

### References

- [1] Attila Kővári: Influence of cylinder leakage on dynamic behavior of electrohydraulic servo system, in Proceedings of 1st IEEE Eastern European Regional Conference on the Engineering of Computer Based Systems, Novi Sad, Serbia, September 7-8, 2009, conference CD ROM
- [2] Attila Kővári: Programming of TMS320F2812 DSP using MATLAB Simulink, in Proceedings of Hungarian Science Week at Collage of Dunaújváros – Informatics Section, Dunaújváros, Hungary, November 12-16, 2007, conference CD ROM
- [3] Richard Poley, “DSP Control of Electro-Hydraulic Servo Actuators”, Texas Instruments Application Report, 2005
- [4] Halmay A., Safta C.A., Ursu I., Ursu F., “Stability of Equilibria in a Four-dimensional Nonlinear Model of a Hydraulic Servomechanism”, Journal of Engineering Mathematics, Volume 49, Number 4, pp. 391-405(15), August 2004